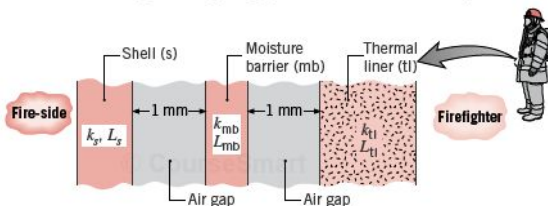


■ Problems

cell is that such a device can internally reform readily available liquid fuels into hydrogen that can then be used to produce electrical power in a manner similar to Example 1.4. Consider a portable solid oxide fuel cell, operating at a temperature of  $T_{fc} = 800^\circ\text{C}$ . The fuel cell is housed within a cylindrical canister of diameter  $D = 75$  mm and length  $L = 120$  mm. The outer surface of the canister is insulated with a low-thermal-conductivity material. For a particular application, it is desired that the thermal signature of the canister be small, to avoid its detection by infrared sensors. The degree to which the canister can be detected with an infrared sensor may be estimated by equating the radiation heat flux emitted from the exterior surface of the canister (Equation 1.5;  $E_s = \epsilon_s \sigma T_s^4$ ) to the heat flux emitted from an equivalent black surface, ( $E_b = \sigma T_b^4$ ). If the equivalent black surface temperature,  $T_b$ , is near the surroundings temperature, the thermal signature of the canister is too small to be detected—the canister is indistinguishable from the surroundings.

- (a) Determine the required thickness of insulation to be applied to the cylindrical wall of the canister to ensure that the canister does not become highly visible to an infrared sensor (i.e.,  $T_b - T_{sur} < 5$  K). Consider cases where (i) the outer surface is covered with a very thin layer of dirt ( $\epsilon_s = 0.90$ ) and (ii) the outer surface is comprised of a very thin polished aluminum sheet ( $\epsilon_s = 0.08$ ). Calculate the required thicknesses for two types of insulating material, calcium silicate ( $k = 0.09$  W/m · K) and aerogel ( $k = 0.006$  W/m · K). The temperatures of the surroundings and the ambient are  $T_{sur} = 300$  K and  $T_\infty = 298$  K, respectively. The outer surface is characterized by a convective heat transfer coefficient of  $h = 12$  W/m<sup>2</sup> · K.
- (b) Calculate the outer surface temperature of the canister for the four cases (high and low thermal conductivity; high and low surface emissivity).
- (c) Calculate the heat loss from the cylindrical walls of the canister for the four cases.

3.19 A firefighter's protective clothing, referred to as a turnout coat, is typically constructed as an ensemble of three layers separated by air gaps, as shown schematically.



Representative dimensions and thermal conductivities for the layers are as follows.

Layer	Thickness (mm)	$k$ (W/m · K)
Shell (s)	0.8	0.047
Moisture barrier (mb)	0.55	0.012
Thermal liner (tl)	3.5	0.038

The air gaps between the layers are 1 mm thick, and heat is transferred by conduction and radiation exchange through the stagnant air. The linearized radiation coefficient for a gap may be approximated as,  $h_{rad} = \sigma(T_1 + T_2)(T_1^2 + T_2^2) \approx 4\sigma T_{avg}^3$ , where  $T_{avg}$  represents the average temperature of the surfaces comprising the gap, and the radiation flux across the gap may be expressed as  $q''_{rad} = h_{rad}(T_1 - T_2)$ .

- (a) Represent the turnout coat by a thermal circuit, labeling all the thermal resistances. Calculate and tabulate the thermal resistances per unit area (m<sup>2</sup> · K/W) for each of the layers, as well as for the conduction and radiation processes in the gaps. Assume that a value of  $T_{avg} = 470$  K may be used to approximate the radiation resistance of both gaps. Comment on the relative magnitudes of the resistances.
- (b) For a pre-flash-over fire environment in which firefighters often work, the typical radiant heat flux on the fire-side of the turnout coat is 0.25 W/cm<sup>2</sup>. What is the outer surface temperature of the turnout coat if the inner surface temperature is 66°C, a condition that would result in burn injury?

Contact Resistance

3.20 A composite wall separates combustion gases at 2600°C from a liquid coolant at 100°C, with gas- and liquid-side convection coefficients of 50 and 1000 W/m<sup>2</sup> · K. The wall is composed of a 10-mm-thick layer of beryllium oxide on the gas side and a 20-mm-thick slab of stainless steel (AISI 304) on the liquid side. The contact resistance between the oxide and the steel is 0.05 m<sup>2</sup> · K/W. What is the heat loss per unit surface area of the composite? Sketch the temperature distribution from the gas to the liquid.

3.21 Two stainless steel plates 10 mm thick are subjected to a contact pressure of 1 bar under vacuum conditions for which there is an overall temperature drop of 100°C across the plates. What is the heat flux through the plates? What is the temperature drop across the contact plane?

3.22 Consider a plane composite wall that is composed of two materials of thermal conductivities  $k_A = 0.1$  W/m · K and